

Unit 4
Module 9.2
Part 1

Rationals:
Operations with Rational Expressions

Objective: Given a rational expression, students will be able to write equivalent expressions.

objective and
corrections

Simplify

$$1. \frac{1}{2} + \frac{2}{7} =$$

$$\begin{array}{r} \frac{1 \cdot 7}{2 \cdot 7} = \frac{7}{14} \\ + \frac{2 \cdot 2}{7 \cdot 2} = \frac{4}{14} \\ \hline \frac{11}{14} \end{array}$$

$$2. \frac{1}{3} - \frac{2}{5} =$$

$$\begin{array}{r} \frac{1 \cdot 5}{3 \cdot 5} = \frac{5}{15} \\ - \frac{2 \cdot 3}{5 \cdot 3} = \frac{6}{15} \\ \hline \frac{-1}{15} \end{array}$$

$$\frac{-1}{15}$$

$$\frac{1}{x+3} + \frac{2}{x-5}$$

$$\frac{3}{x+5} - \frac{-x}{x-6}$$

~~W~~
 Monday
 Tuesday
 Wednesday
 Thursday
 Friday

Vocabulary

Rational Expression: An expression of the form $\frac{p(x)}{q(x)}$ where $p(x)$ and $q(x)$ are polynomials and $q(x)$ is not zero.

The **excluded values** for a rational expression are any values of the variable for which the expression is undefined.

The **expressions are equivalent** provided they have the same value for every value of the variable unless they are both undefined for that value of the variable.

$$\frac{1}{2} = \frac{7}{14}$$

$$\frac{2 \cdot 2}{x \cdot 2} = \frac{4}{2x}$$

$$-\frac{1 \cdot 5}{(x+5) \cdot (-5)} = \frac{5}{-5x-15}$$

Find an equivalent expression

$$\frac{3}{(x+4)} = \frac{1 \cdot 3}{4x+16} \Leftarrow$$

Example

Make equivalent expressions.

$$\frac{1}{x-2} = \frac{?}{(x-2)(x+6)}$$

$$\frac{1 \cdot (x+6)}{(x-2) \cdot (x+6)} = \frac{x+6}{(x-2)(x+6)}$$

What are the excluded values for the simplified expression for which the expression would be undefined?

$$x \neq 2$$

$$x \neq -6$$

Example

Make equivalent expressions.

$$\frac{2}{x-9} = \frac{?}{(x-9)(x+4)}$$

What are the excluded values for the simplified expression for which the expression would be undefined?

$$\frac{2 \cancel{(x+4)}}{x-9} = \frac{2x? + 8}{(x-9)(x+4)}$$

$$x \neq 9$$

$$x \neq -4$$

Example

Make equivalent expressions.

$$\frac{-3}{x-4} = \frac{?}{(x-4)(x+6)}$$

What are the excluded values for the simplified expression for which the expression would be undefined?

$$\frac{-3 \cancel{(x+6)}}{x-4} = \frac{3x? + 18}{(x-4)(x+6)}$$

$$x \neq 4$$

$$x \neq -6$$

Example

Make equivalent expressions.

$$\frac{-x}{x-5} = \frac{?}{(x-1)(x-5)}$$

What are the excluded values for the simplified expression for which the expression would be undefined?

$$\frac{-x \overset{(x-1)}{\cancel{}}}{x-5} = \frac{\overset{(x-1)}{\cancel{-x^2}} \overset{(x-1)}{\cancel{?}} \overset{(x-1)}{\cancel{x}}}{(x-1)(x-5)}$$

$$x \neq 1$$

$$x \neq 5$$

Example

Simplify.

$$\frac{x-4}{(x-3)} = \frac{?}{(x-3)(x+2)}$$

What are the excluded values for the simplified expression for which the expression would be undefined?

Example

Simplify.

$$\frac{1}{x+2} - \frac{4}{x-1}$$

What are the excluded values for the simplified expression for which the expression would be undefined?

Tommy